

## Suma y resta de ángulos:

$$\text{sen}(\alpha \pm \beta) = \text{sen}\alpha \cdot \cos\beta \pm \cos\alpha \cdot \text{sen}\beta$$

$$\cos(\alpha \pm \beta) = \cos\alpha \cdot \cos\beta \mp \text{sen}\alpha \cdot \text{sen}\beta$$

$$\text{tg}(\alpha \pm \beta) = \frac{\text{tg}\alpha \pm \text{tg}\beta}{1 \mp \text{tg}\alpha \cdot \text{tg}\beta}$$

## Ángulo doble:

$$\text{sen}(2\alpha) = 2\text{sen}\alpha \cdot \cos\alpha$$

$$\cos(2\alpha) = \cos^2\alpha - \text{sen}^2\alpha$$

$$\text{tg}(2\alpha) = \frac{2\text{tg}\alpha}{1 - \text{tg}^2\alpha}$$

## Ángulo mitad

$$\text{sen}\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos\alpha}{2}}$$

$$\cos\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 + \cos\alpha}{2}}$$

$$\text{tg}\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos\alpha}{1 + \cos\alpha}}$$